



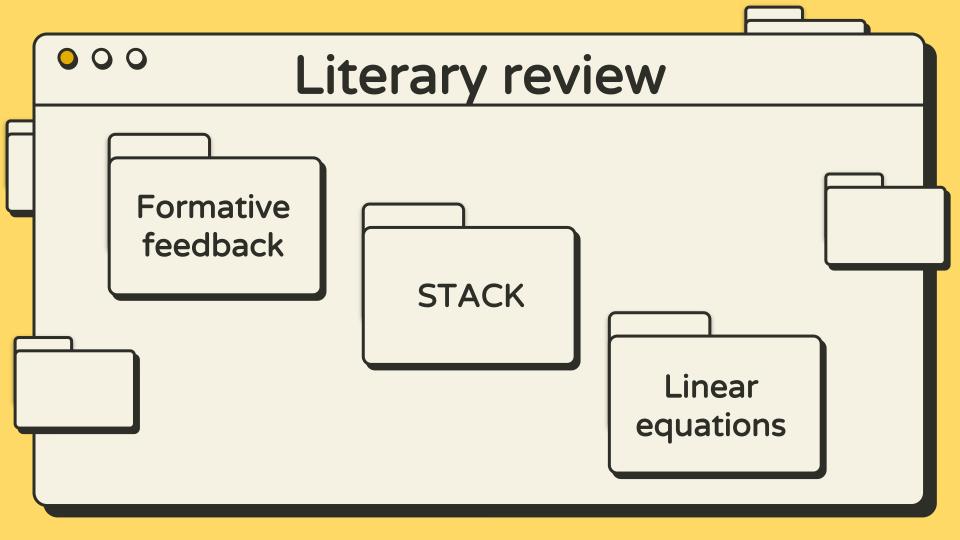




Formative feedback on linear equations

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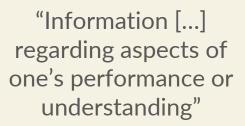
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Literary review: formative feedback



Feedback





Types

- □ Sumative/**formative** /based on practices
- □ **Immediate**/delayed...



Given...

...after initial instruction. □ Conceptual/procedural "Feedback has no effect in

a vacuum".

It has to be useful.

Hattie & Timperley (2007)



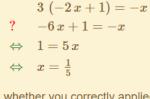
Literary review: STACK



Answer: algebraic expressions



Encoding of typical mistakes



Check whether you correctly applied the distributive property. Did you multiply the factor outside of the parentheses by each of the ones inside?



Specific feedback

Sangwin (2015); Pinkernell et al. (2023)



Literary review: linear equations

Distributive property

Expand A(Bx+C)

Addition

Add/subtract the same term on both sides

Multiplication

Multiply/divide by the same factor on both sides

Common denominator

Add fractional numbers

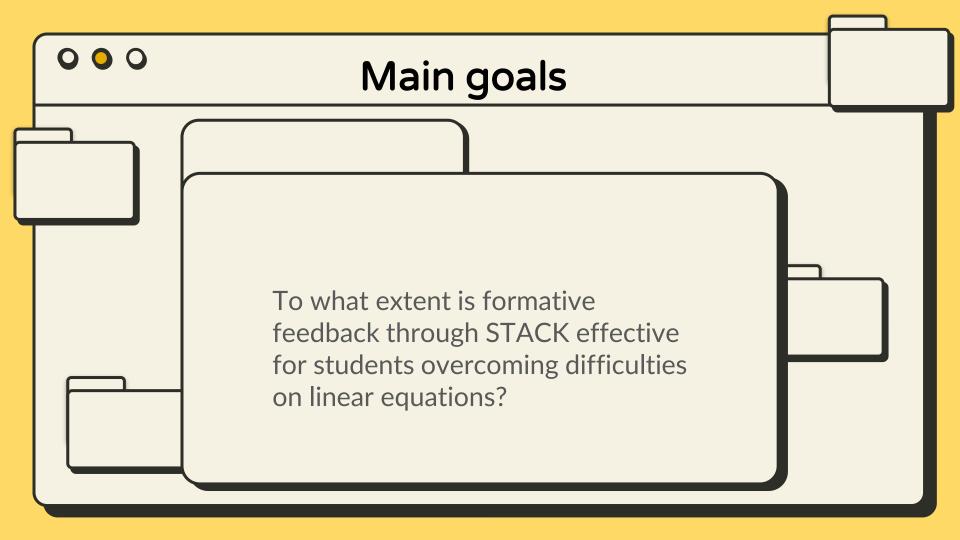
Coeff-var separation

 $Ax \rightarrow A+x$

Arithmetic

Basic arithmetic operations

Pérez et al. (2019)





Methodology

Sample

132 students:

- □ 39 in secondary school (aged 14-16)
- 93 who have finished secondary school

Average achievers – some especially struggled



Cantabria, Spain



Methodology

Equations

a)
$$3(-2x+1)=-x$$

b)
$$\frac{7}{2}x = 14$$

c)
$$-4x=16$$

d)
$$-2(3x-4)=10$$

e)
$$\frac{x}{3} + 2x = 7$$

f)
$$-3x+5=17$$

Feedback

$$3(-2x+1) = -x$$

?
$$-6x + 1 = -x$$

$$\Leftrightarrow 1 = 5x$$

$$\Leftrightarrow x = \frac{1}{5}$$

Check whether you correctly applied the distributive property. Did you multiply the factor outside of the parentheses by each of the ones inside?



Pérez et al. (2019)







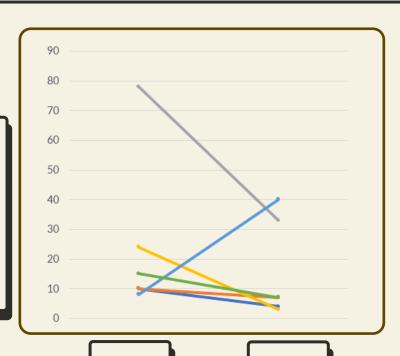
Results

Multiplication

Students tried to solve Ax=B as:

- \Box x=B/A
- \Box x=-B/A
- \Box x=A/B
- \Box x=-A/B

Number of mistakes



Start

Finish



Results

Common denominator

Students avoided using common denominator:

$$\frac{7}{2}x = 14$$

$$\Leftrightarrow 7x = 28$$

$$\Leftrightarrow x = \frac{28}{7}$$

$$\Leftrightarrow x = 4$$

$$\frac{x}{3} + 2x = 7$$

$$\Leftrightarrow \frac{x}{3} = 7 - 2x$$

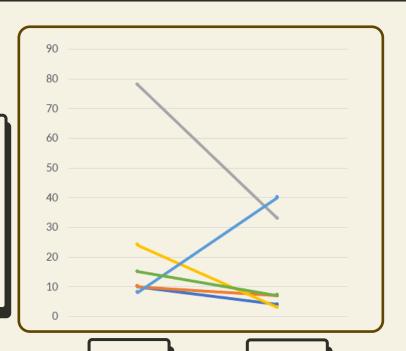
$$\Leftrightarrow x = 3(7 - 2x)$$

$$\Leftrightarrow x = 21 - 6x$$

$$\Leftrightarrow 7x = 21$$

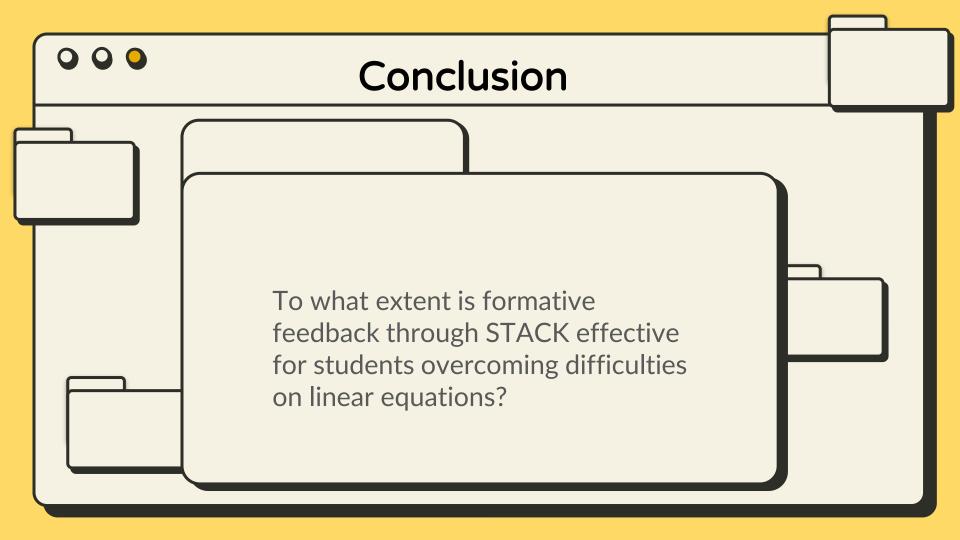
$$\Leftrightarrow x = 3$$

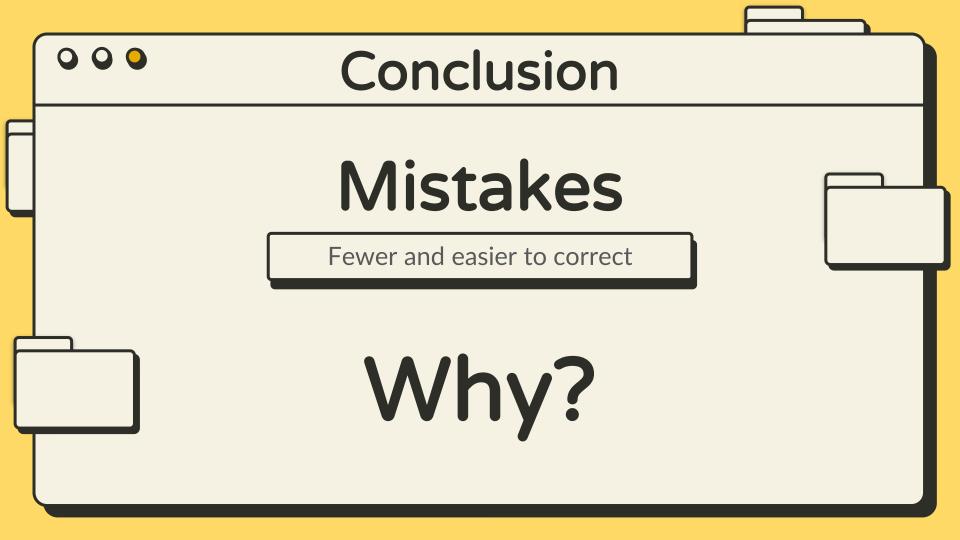
Number of mistakes



Start

Finish







Conclusion

Mistakes

Fewer and easier to correct

Feedback

□ Immediate

Computer → objective

Only after the mistakes

□ Focused on the task

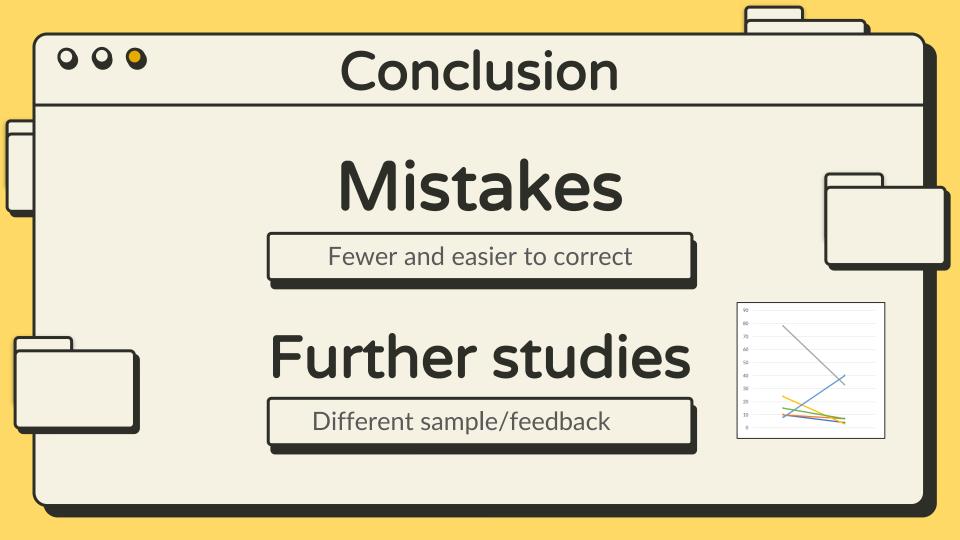
☐ Short, clear and specific

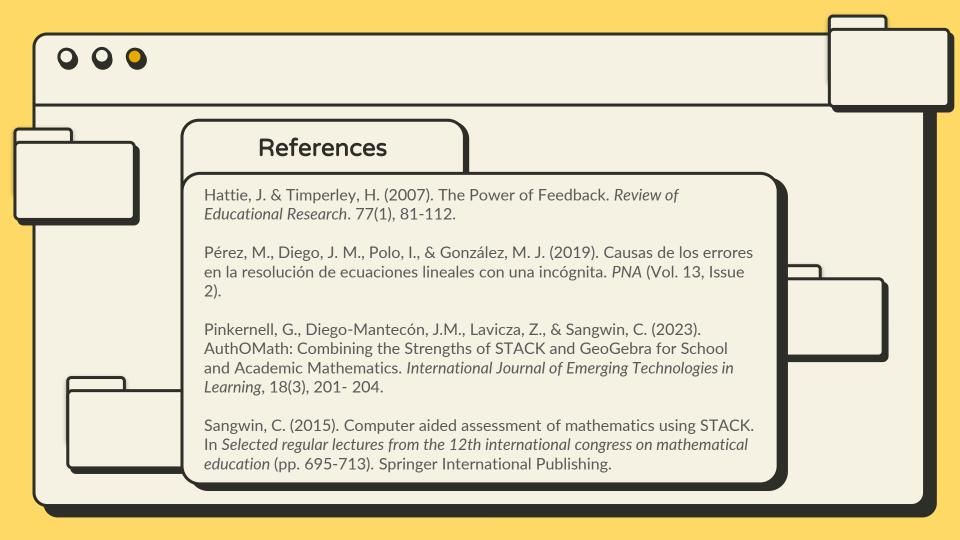
Try again

Not providing grades

Prior knowledge

STACK













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